

Office hours today: after class in Remo

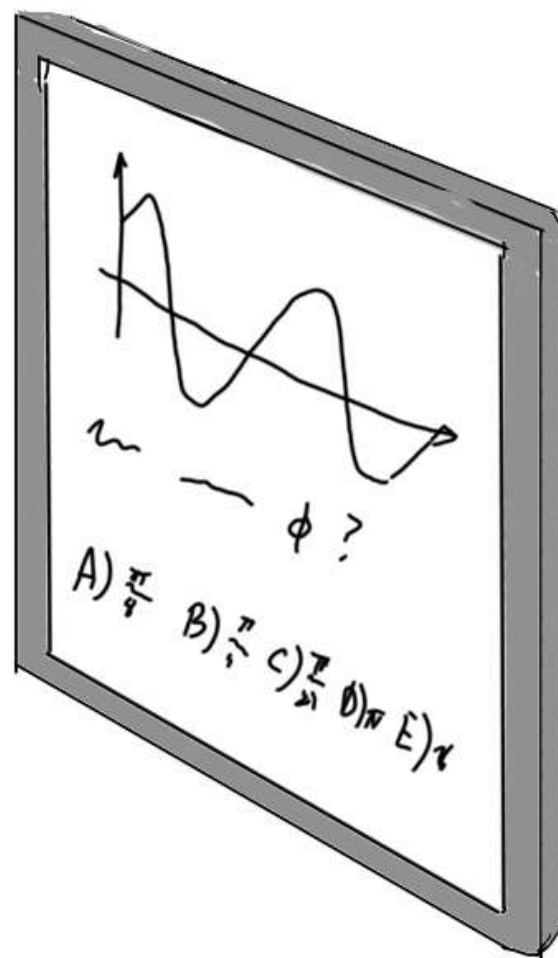
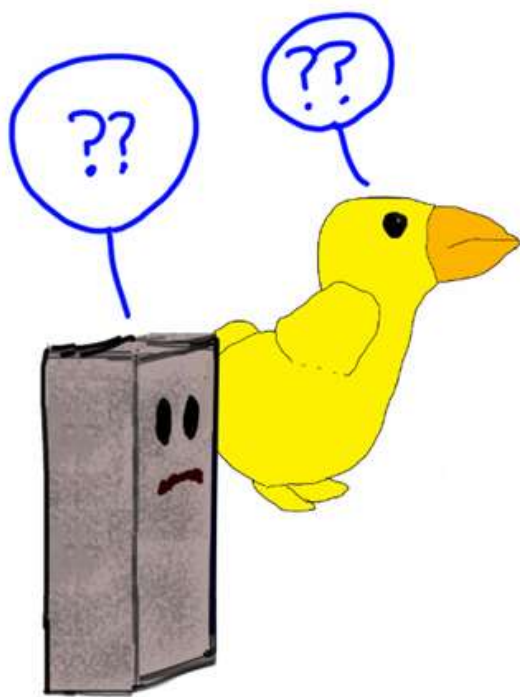
Reminder: quiz Thursday (entropy and oscillations)

Learning goals for today:

To predict the equilibrium position of a system by calculating the various contributions to net force and requiring that the net force vanishes.

To predict the oscillation frequency of a system given the net force as a function of position or given physical information that permits the calculation of net force as a function of position.

Last time in Phys 157..



A 1 kg mass sits on a spring with $k=1000\text{N/m}$. If we add another 1kg mass on top, the amount by which the equilibrium position changes is:

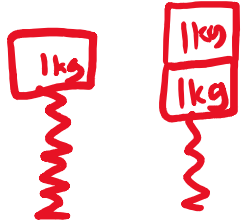
A) 1cm

B) 2cm

C) 10cm

D) 1m

E) It can't be determined without knowing the unstretched length of the spring.



A 1 kg mass sits on a spring with $k=1000\text{N/m}$. If we add another 1kg mass on top, the amount by which the equilibrium position changes is about:

At equilibrium, compression of the spring is determined by $F_{\text{NET}} = 0$

$$mg = kx$$

With different masses, $m_1 g = kx_1$, and $m_2 g = kx_2$, so when we add the extra mass, $\Delta m \cdot g = k \cdot \Delta x$. Thus: $\Delta x = \frac{\Delta m g}{k} = 1\text{cm}$

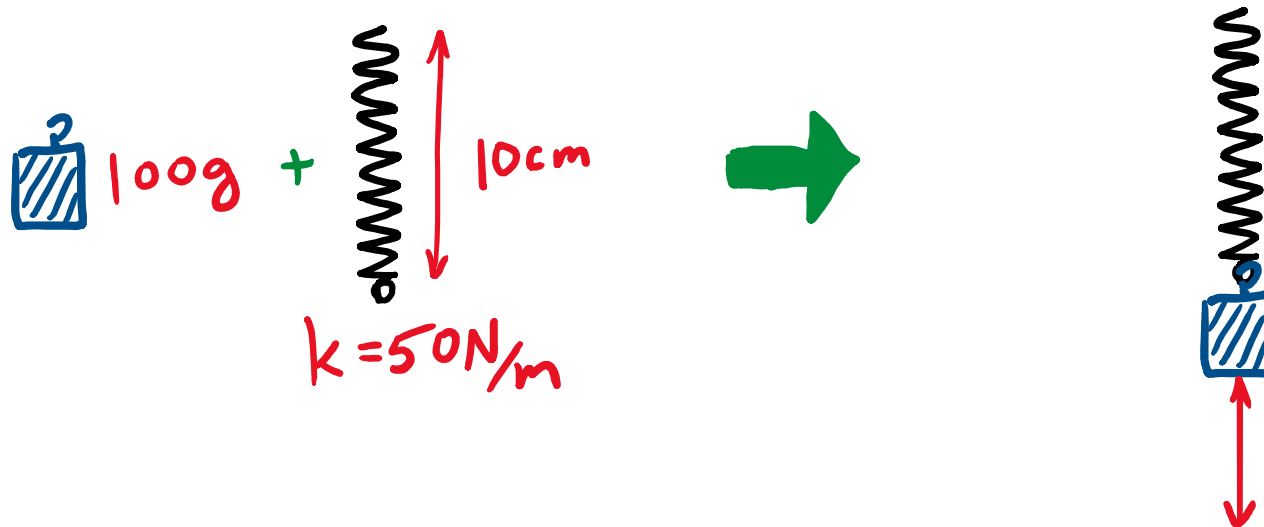
A) 1cm

B) 2cm

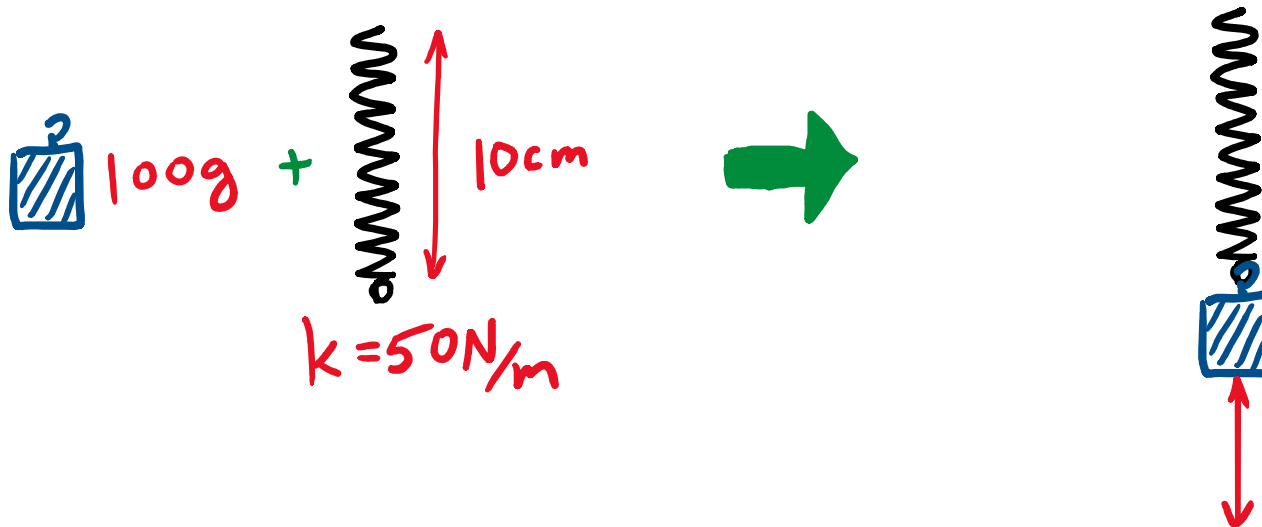
C) 10cm

D) 1m

E) It can't be determined without knowing the unstretched length of the spring.



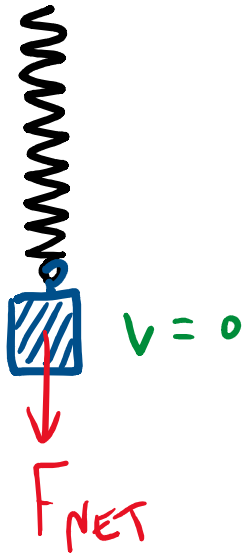
Discussion question: A 10cm long spring has a spring constant of 20 N/m. If we attach a 100g weight to the spring and release it, what will be the amplitude of the resulting oscillation?



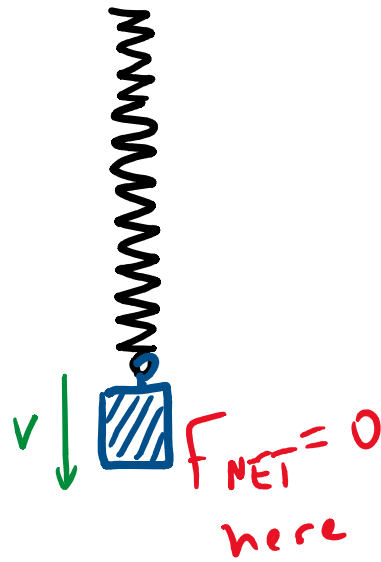
Discussion question: A 10cm long spring has a spring constant of 20 N/m. If we attach a 100g weight to the spring and release it, what will be the amplitude of the resulting oscillation?

- A) 1cm B) 2cm C) 3cm D) 4cm E) 5cm

top (initial)



middle

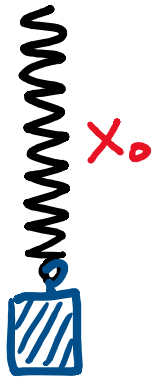


bottom

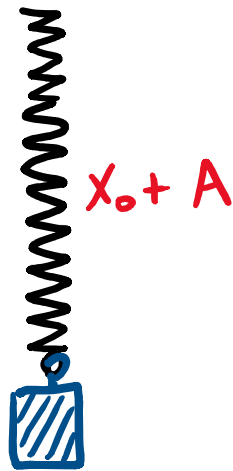


this is also
the equilibrium
position

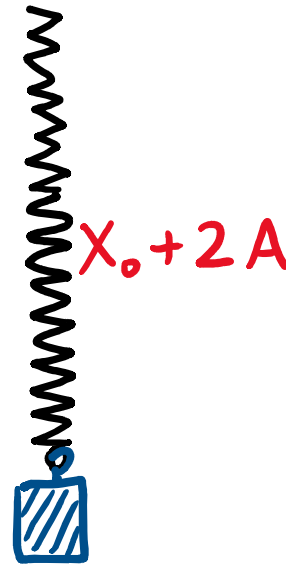
top (initial)



middle



bottom



Middle position is equilibrium position,
so $F_{NET} = mg - kA = 0$ here.

$$A = \frac{mg}{k} = \frac{1\text{N}}{50\text{N/m}} = 2\text{cm}$$

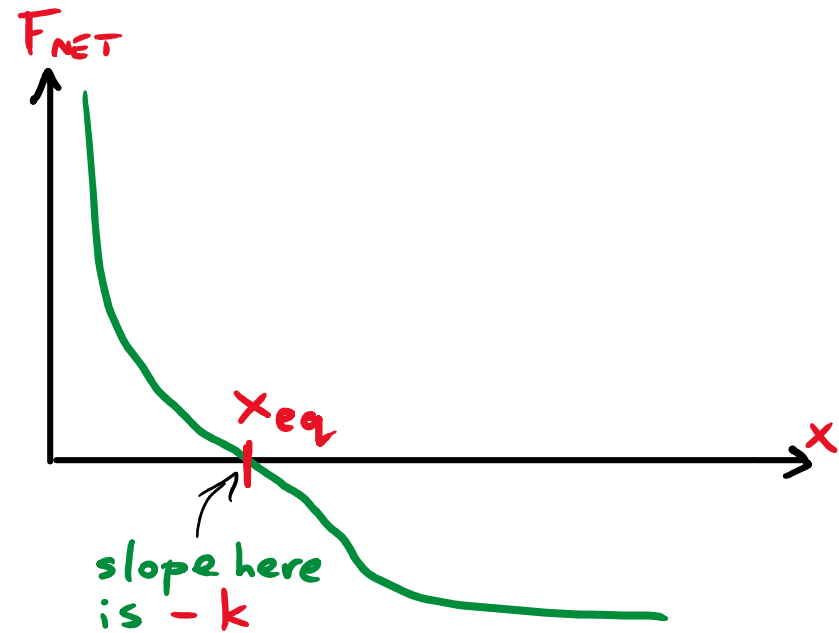
How to find ω in examples:

① Find F_{NET} as a function of position x

② Find equilibrium value x_{eq}
by solving $F_{NET}(x_{eq}) = 0$.

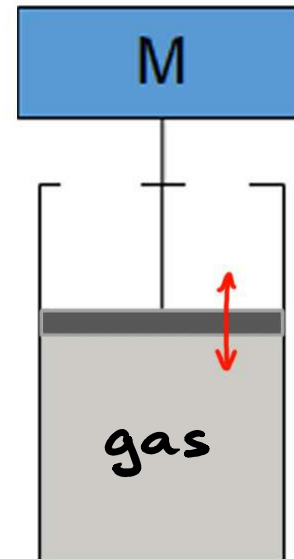
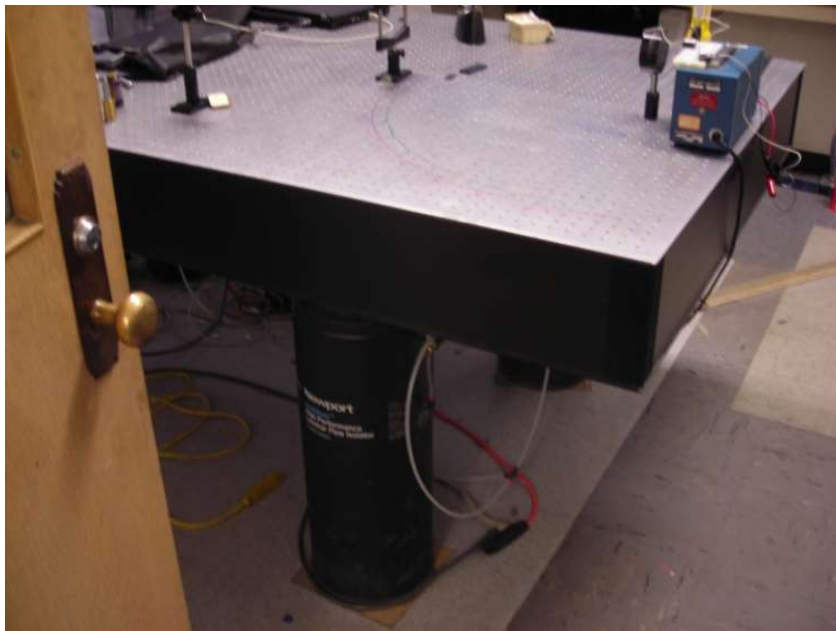
③ $-k$ is $F'_{NET}(x_{eq})$, the
slope at x_{eq} .

④ Then $\omega = \sqrt{\frac{k}{m}}$



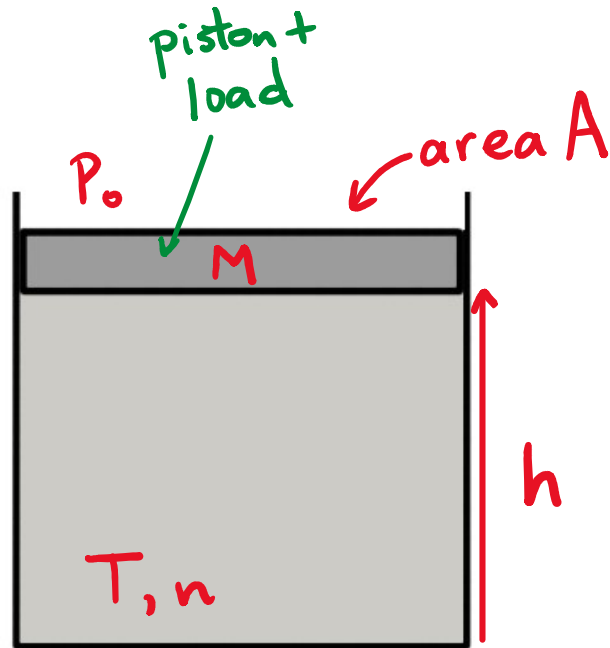
Example: air leg

- used to isolate sensitive equipment from vibration.



assume: any motion of piston is slow
so compression/expansion is isothermal

Example: air leg



$$P_0 = 100 \text{ kPa}$$

$$M = 200 \text{ kg}$$

$$g \approx 10 \text{ m/s}^2$$

$$A = 0.03 \text{ m}^2$$

$$T = 300 \text{ K}$$

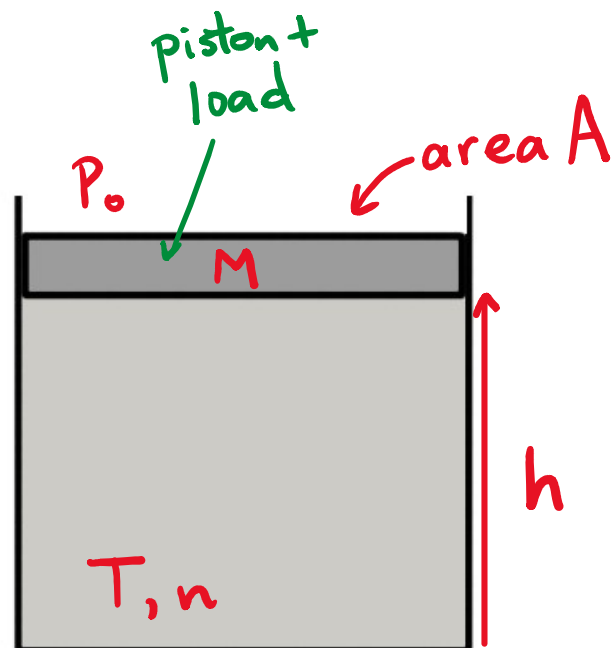
$$nR = 5 \text{ J/K}$$

a) Draw a free body diagram for the object of mass M showing the vertical forces.

b) Calculate the magnitude of the net upwards force on the object as a function of the height h of the piston.

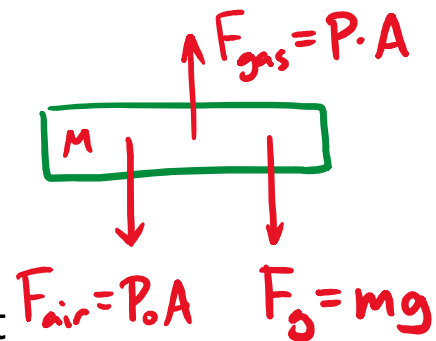
Your answer should be a function of h

Example: air leg



$$\begin{aligned}P_0 &= 100 \text{ kPa} \\M &= 200 \text{ kg} \\g &\approx 10 \text{ m/s}^2 \\A &= 0.03 \text{ m}^2 \\T &= 300 \text{ K} \\nR &= 5 \text{ J/K}\end{aligned}$$

a) Draw a free body diagram for the object of mass M showing the vertical forces.

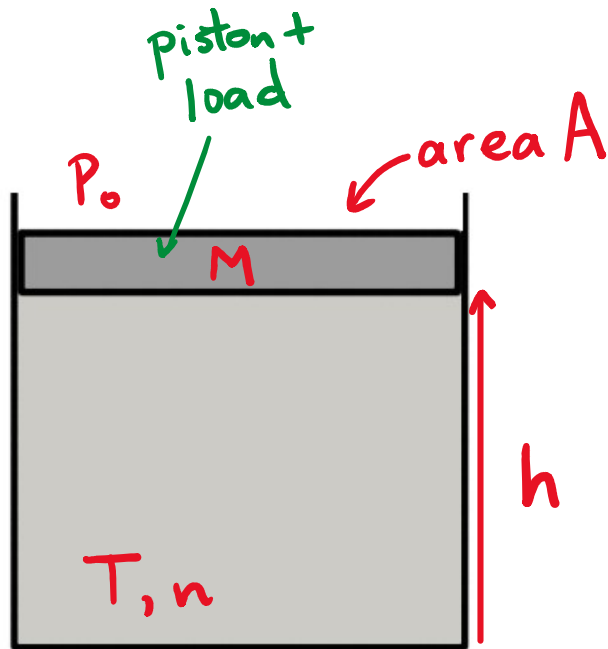


b) Calculate the magnitude of the net upwards force on the object as a function of the height h of the piston.

$$\begin{aligned}\text{Have: } P &= \frac{nRT}{V} = \frac{nRT}{A \cdot h} \\ \text{so } F_{\text{gas}} &= PA = \frac{nRT}{h}\end{aligned}$$

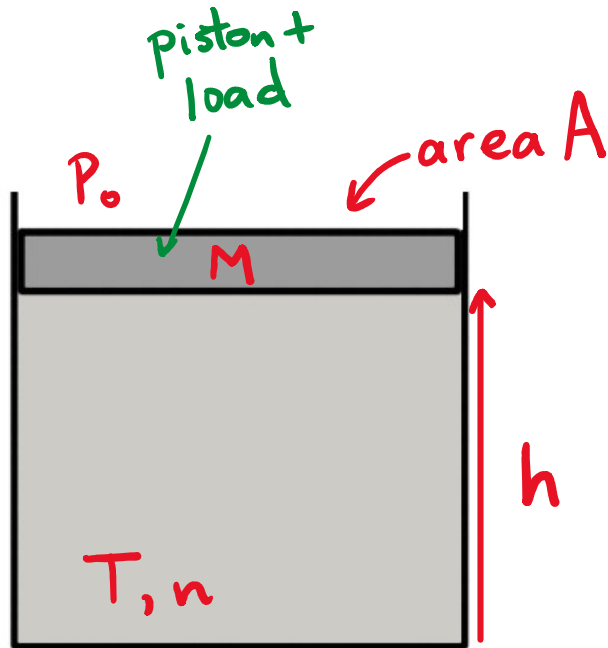
$$F_{\text{NET}}^{\text{up}} = \frac{nRT}{h} - P_0 A - mg = \frac{1500 \text{ J}}{h} - 5000 \text{ N}$$

Example: air leg

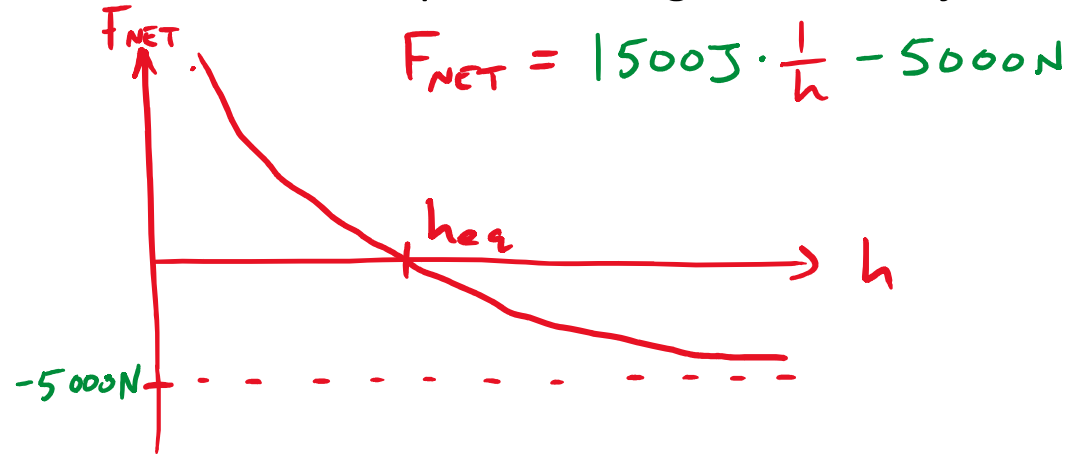


c) Graph this upward force as a function of h , for positive values of h up to the height of the object.

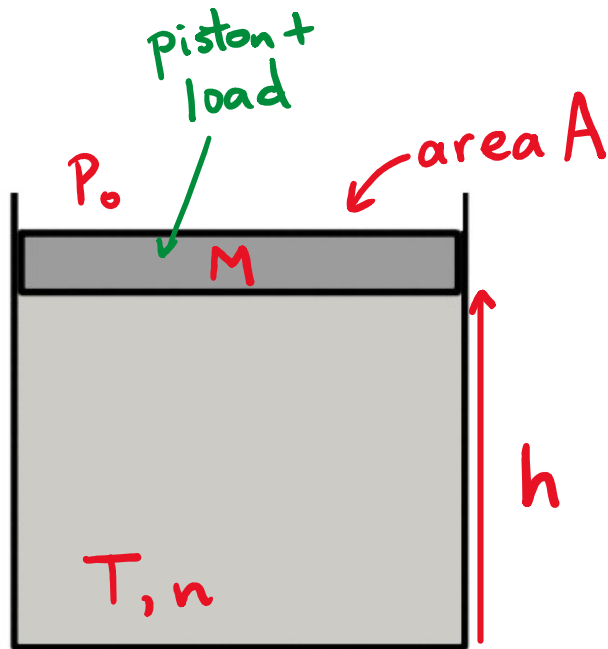
Example: air leg



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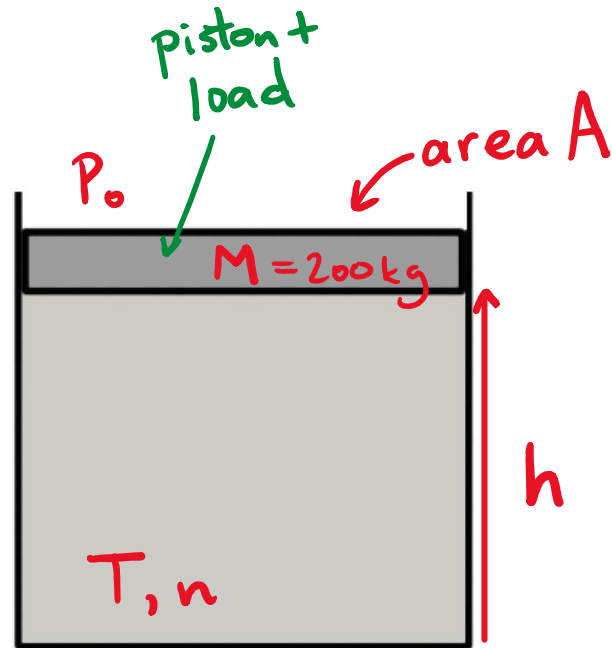
Example: air leg



d) What is the equilibrium height of the piston?

e) What is the oscillation frequency f ?

Example: air leg

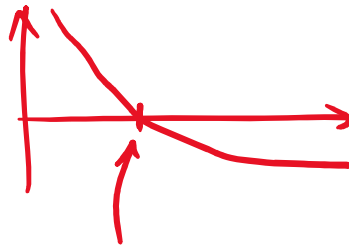


d) What is the equilibrium height of the piston?

equilibrium height: $F_{\text{NET}} = 0$

$h_{\text{eq}} = 0.3 \text{ m}$

e) What is the oscillation frequency f ?



$$k = -\frac{dF}{dh} \text{ at } h_{\text{eq}} = \frac{1500 \text{ J}}{h_{\text{eq}}^2} = 1.67 \times 10^4 \text{ N/m}$$

$$F_{\text{NET}} = \frac{1500 \text{ J}}{h} - 5000 \text{ N}$$

$$\rightarrow \omega = \sqrt{\frac{k}{m}} = 9.1 \text{ s}^{-1}$$

$$f = \frac{\omega}{2\pi} = 1.45 \text{ s}^{-1}$$