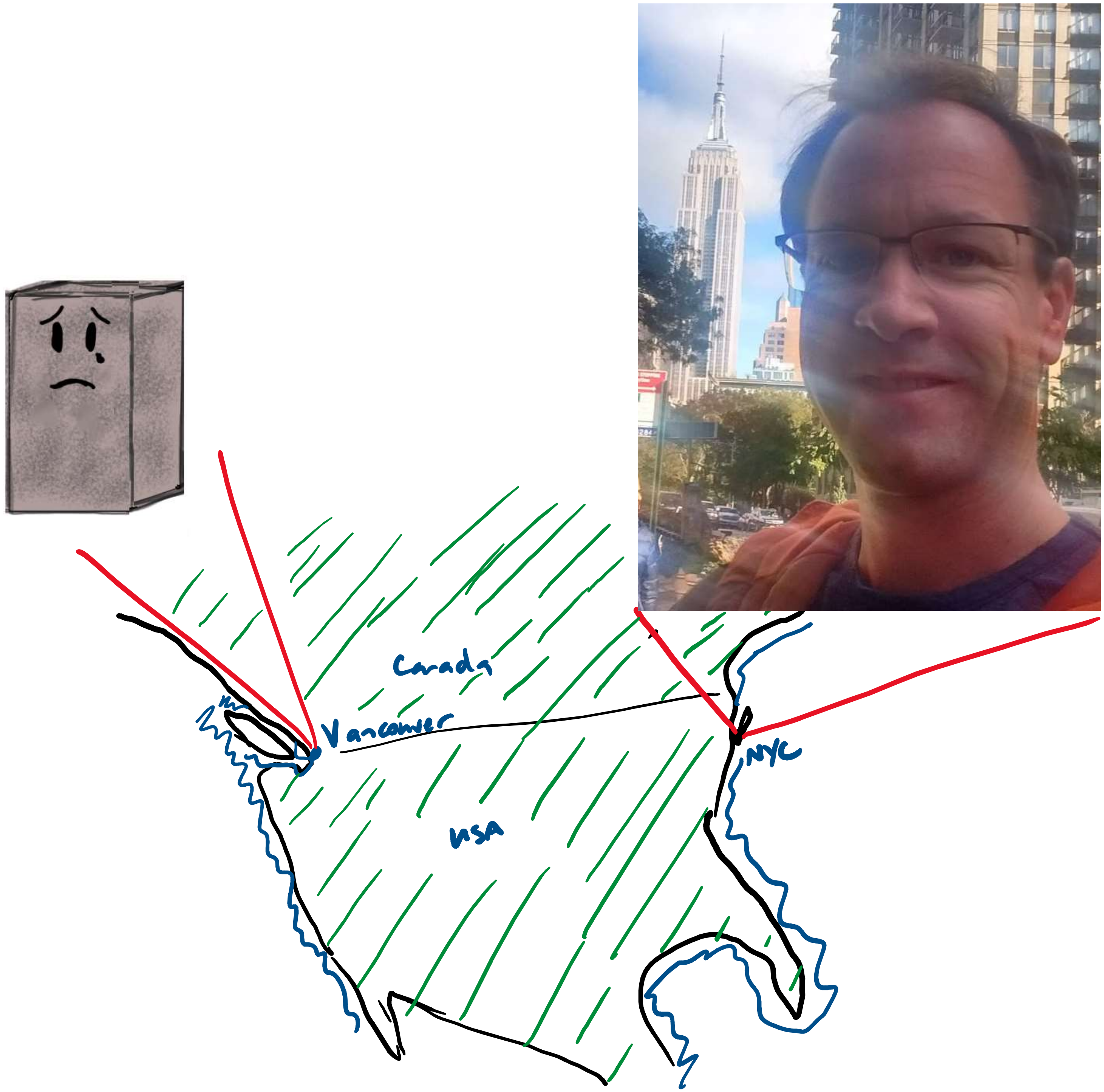
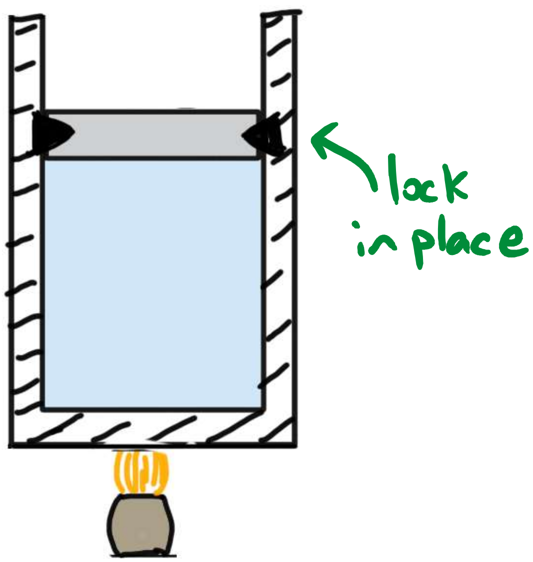
Learning goals:

- For isochoric, isobaric, isothermal, and adiabatic processes, to calculate final temperatures, pressures, and volumes given initial temperatures, pressures and volumes
- For isochoric, isobaric, isothermal, and adiabatic processes, to calculate work done, change in internal energy, and heat added during the process
- Describe qualitatively the difference between adiabatic and isothermal compression and distinguish the graphs of these processes on a PV diagram

Last time in Physics 157...



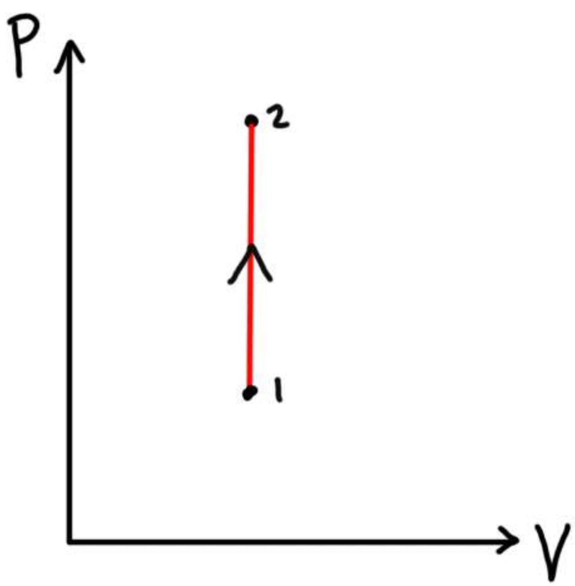
Constant Volume:



Ideal gas law → $\frac{T_2}{T_1} = \frac{P_2}{P_1}$

$W = 0$ so

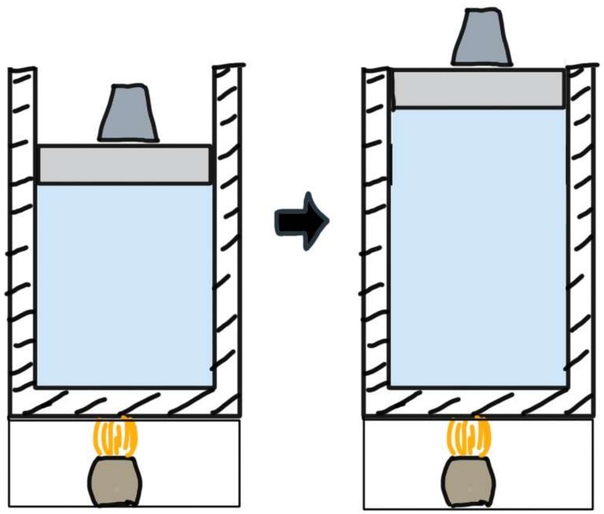
$Q = \Delta U = nC_v \Delta T$

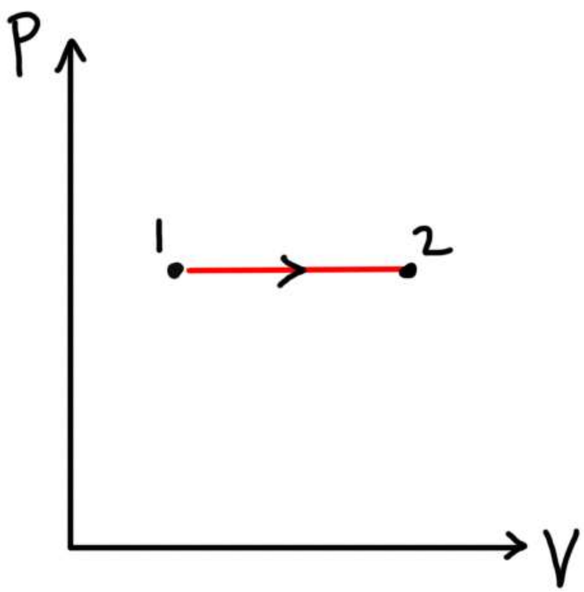


"isochoric"

Constant Pressure

Ideal Gas Law ⇒ $\frac{T_2}{T_1} = \frac{V_2}{V_1}$





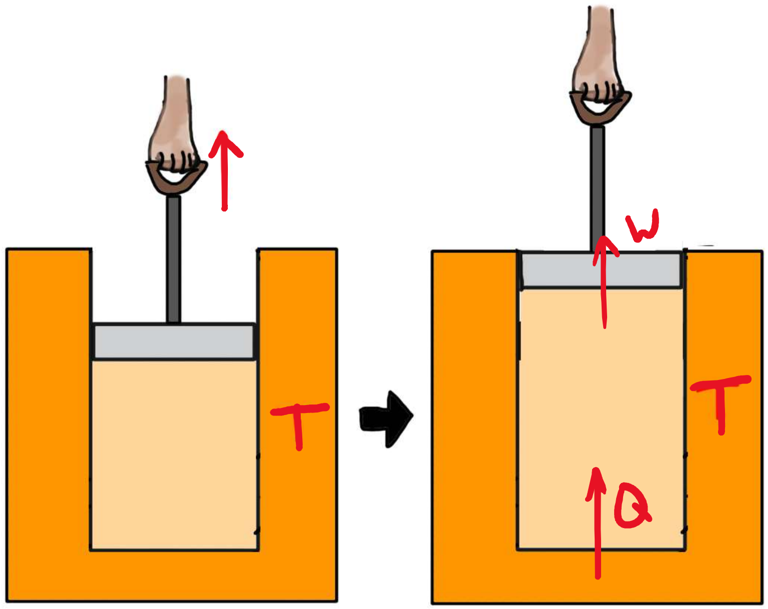
$$W = P\Delta V$$

$$Q = nC_p\Delta T$$

$C_p = C_v + R$

"isobaric"

Constant Temperature



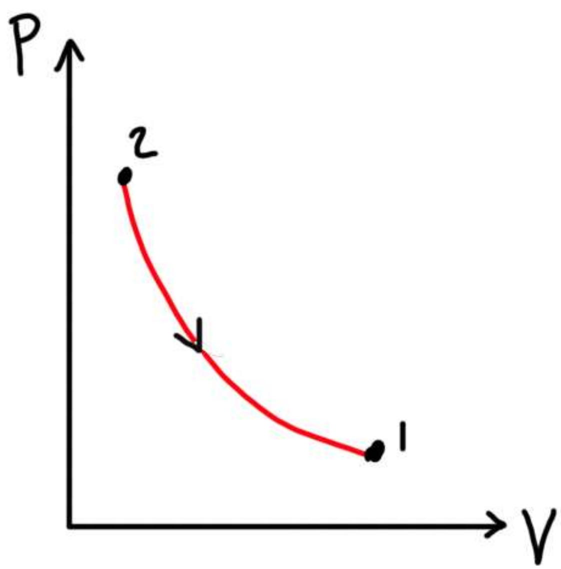
Ideal Gas Law ⇒ $PV = \text{const.}$

so $P \propto \frac{1}{V}$

$$\Delta U = 0$$

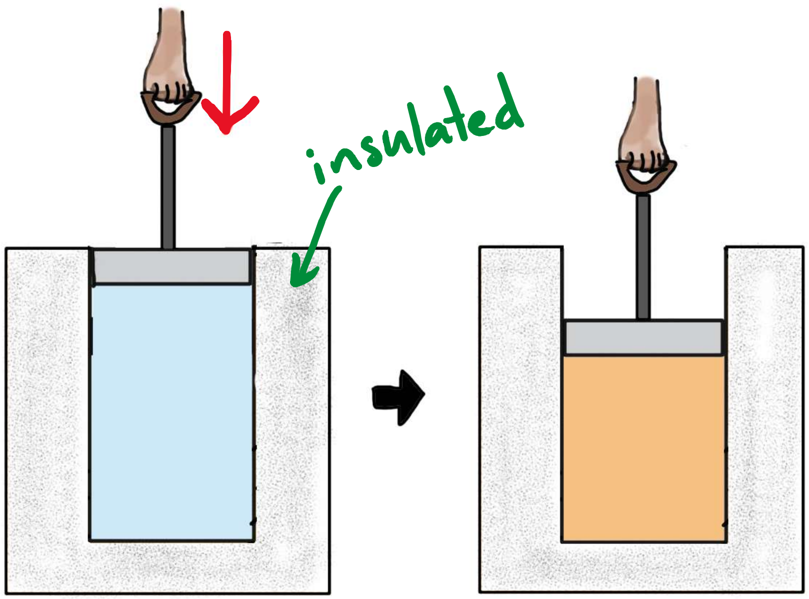
$$Q = W = nRT \ln\left(\frac{V_f}{V_i}\right)$$

$$\int_{V_i}^{V_f} P(V)\,dV$$



"isothermal"

ADIABATIC: $Q = 0$ (insulated or very fast)



First Law: $\Delta U = -W$

compressed gas heats up!

$$nC_v \Delta T = -W$$

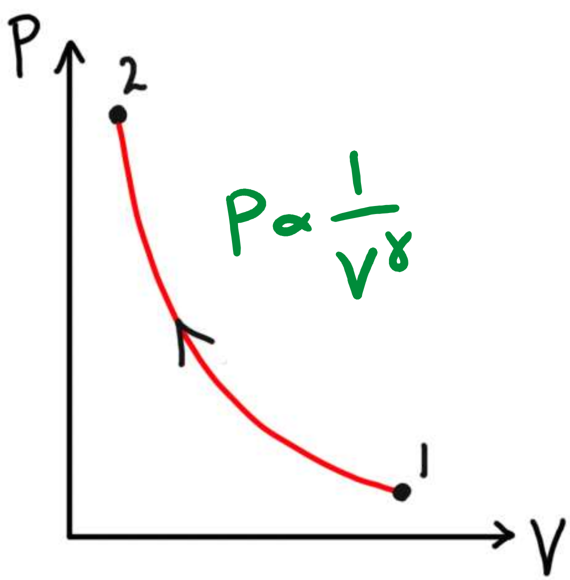
+ ideal gas law

$\frac{PV}{T} =$ constant

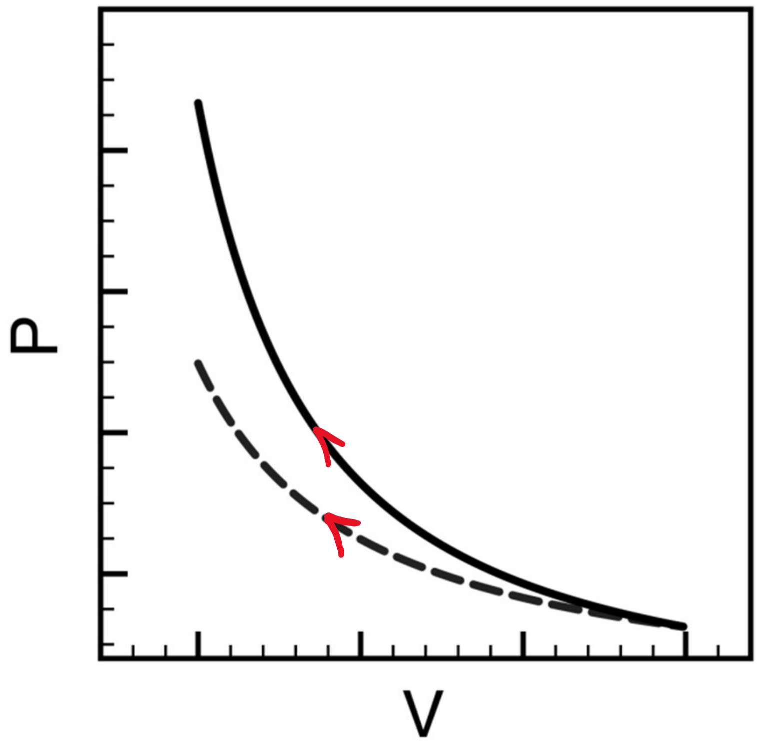
$$PV^{\gamma} = \text{constant}$$

$$TV^{\gamma-1} = \text{constant}$$

see 19.8 or video derivation



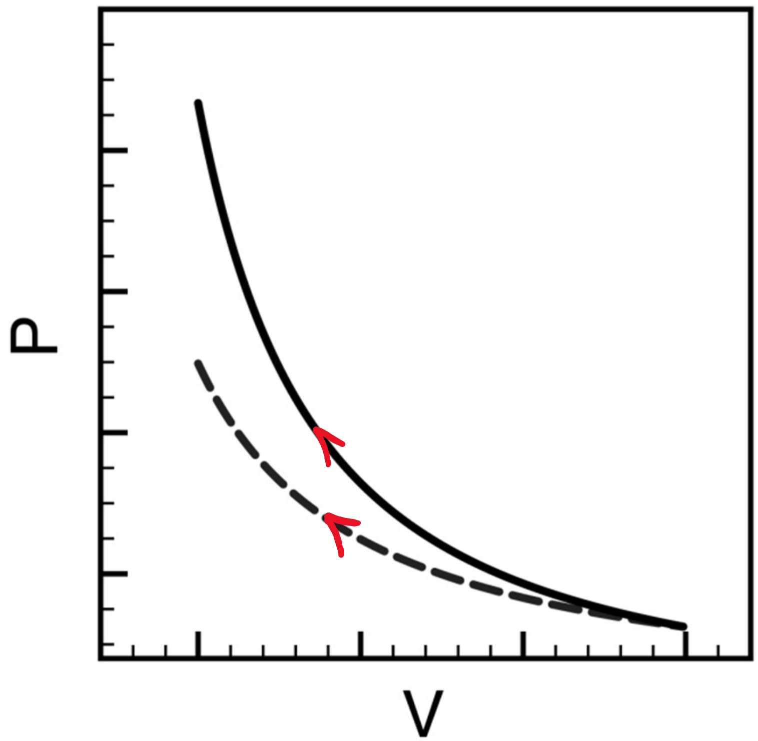
$$\gamma = \frac{C_p}{C_v}$$



In the two processes shown, gas is compressed adiabatically in one case and isothermally in the other. We can say that

A) The solid line represents the isothermal process
B) The solid line represents the adiabatic process
C) We don't have enough information to tell which process is which.

EXTRA: Can you give a conceptual explanation for your answer?



In the two processes shown, gas is compressed adiabatically in one case and isothermally in the other. We can say that

A) The solid line represents the isothermal process
B) The solid line represents the adiabatic process
C) We don't have enough information to tell which process is which.

Method 1:

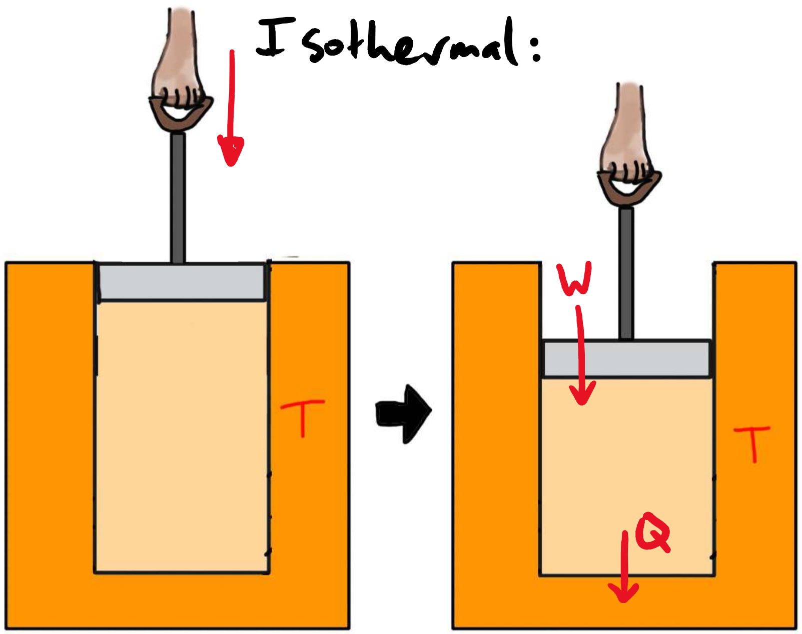
$P \propto \frac{1}{V}$ for isothermal

$P \propto \frac{1}{V^\gamma}$ for adiabatic $\gamma > 1$ so P increases more quickly as V decreases

EXTRA: Can you give a conceptual explanation for your answer?

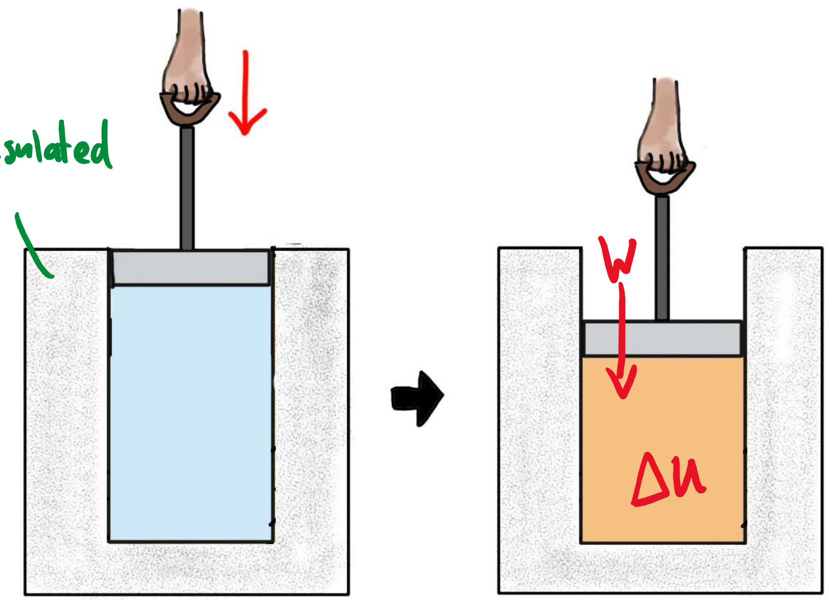
conclusion: adiabatic is solid

Isothermal:



$\Delta U = 0$

insulated



Adiabatic

$\Delta U > 0$ so $T \uparrow$

Method 2:

- same final volume
- higher T

higher final P for adiabatic

Answer is

B

Gas with $C_V = 3\ R$, initially at room temperature, is compressed very rapidly in a cylinder. The **compression ratio** is 15.

a) Estimate the final temperature of the gas.

b) If the tube contains 0.0004 moles of gas, how much work was required to compress the gas?

Gas with $C_V = 3\,R$, initially at room temperature, is compressed very rapidly in a cylinder. The **compression ratio** is 15.

a) Estimate the final temperature of the gas.

The final temperature of the gas is

A) $293\text{K} \cdot (15)^{5/3}$
B) $293\text{K} \cdot (15)^{4/3}$
C) $293\text{K} \cdot (15)$
D) $293\text{K} \cdot (15)^{2/3}$
E) $293\text{K} \cdot (15)^{1/3}$

Gas with $C_V = 3$ R, initially at room temperature and atmospheric pressure, is compressed very rapidly in a cylinder. The **compression ratio** is 15.

a) **Estimate the final temperature of the gas.**

b) If the tube contains 0.0004 moles of gas, how much work was required to compress the gas?

$$\gamma = \frac{C_P}{C_V} = \frac{C_V + R}{C_V} = \frac{4R}{3R} = \frac{4}{3}$$

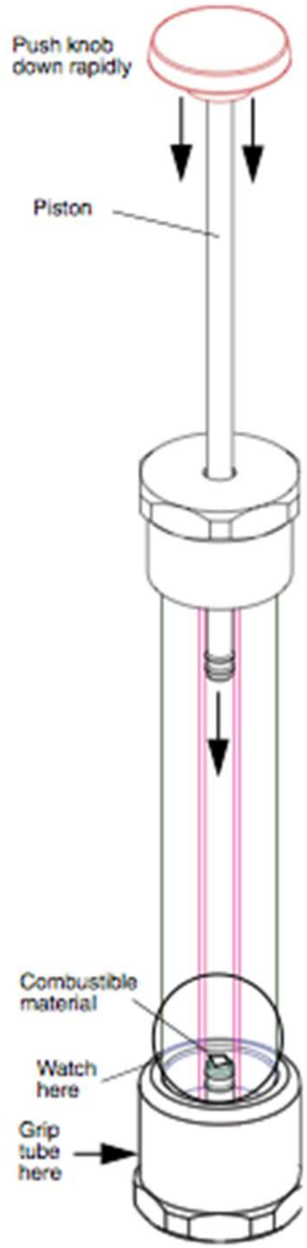
Have $TV^{\gamma-1}$ constant

$$T_2 V_2^{\gamma-1} = T_1 V_1^{\gamma-1}$$

$$T_2 = T_1 \left(\frac{V_1}{V_2}\right)^{\gamma-1} = 293\text{K} \cdot (15)^{\frac{1}{3}}$$

$$= 723\text{K}$$

answer E



Demo: we can ignite cotton just by compressing the air!

Gas with $C_V = 3\,R$, initially at room temperature and atmospheric pressure, is compressed very rapidly in a cylinder. The **compression ratio** is 15.

a) Estimate the final temperature of the gas.

b) If the tube contains 0.0004 moles of gas, how much work was required to compress the gas?

Have $Q = 0$ so:

$$\Delta U = -W_{gas} = W_{\text{done on gas}}$$

So work done equals $\Delta U = n C_v \Delta T$

$$= 0.0004 \cdot 3 \cdot 8.31 \cdot 430\,\text{J}$$

$$= 4.3\,\text{J}$$