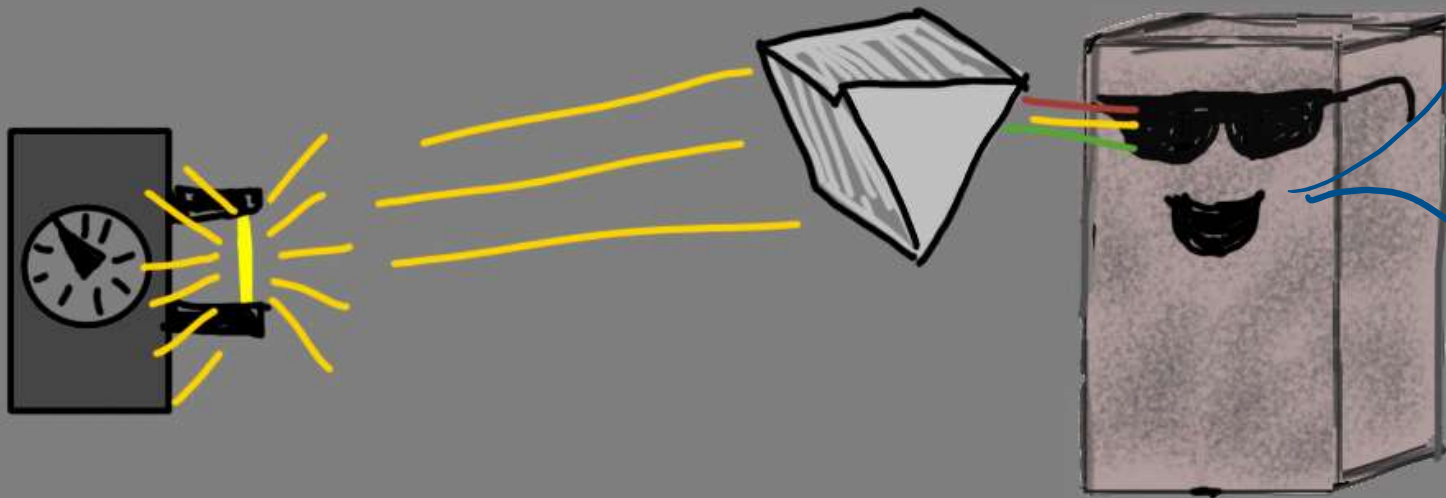
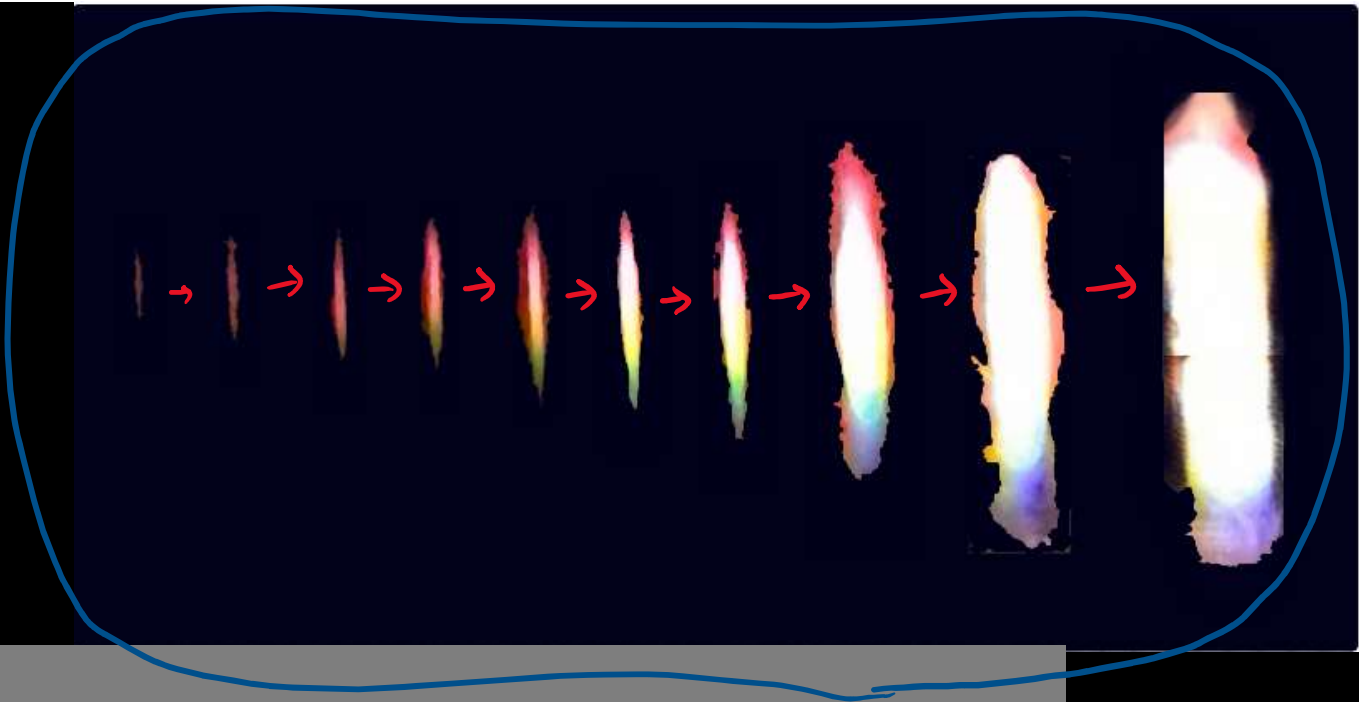


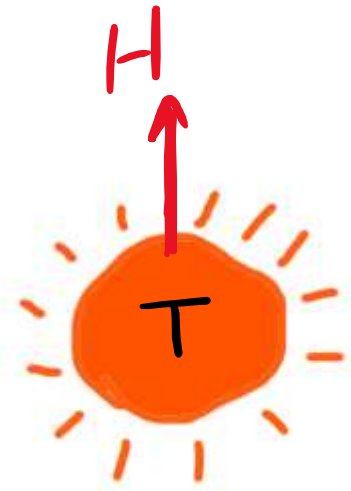
## Learning Goals

- Calculate the equilibrium temperature of a radiating object (e.g. the Earth) by equating the ingoing and outgoing energy currents
- Describe what is meant by intensity of radiation
- Calculate the intensity of radiation at some distance from an object radiating symmetrically in all directions
- Describe how the intensity of radiation changes if we change the distance from the source, for a source radiating uniformly in all directions
- Predict the rate of energy absorbed by an object given its shape and orientation, its albedo, and the intensity of incident radiation
- Explain why the presence of greenhouse gases in the atmosphere of Earth lower its effective emissivity



Last  
time  
in  
Physics  
157...

# TOTAL POWER FROM THERMAL RADIATION



heat current

surface area

$$H = A \cdot e \cdot \sigma \cdot T^4$$

emissivity

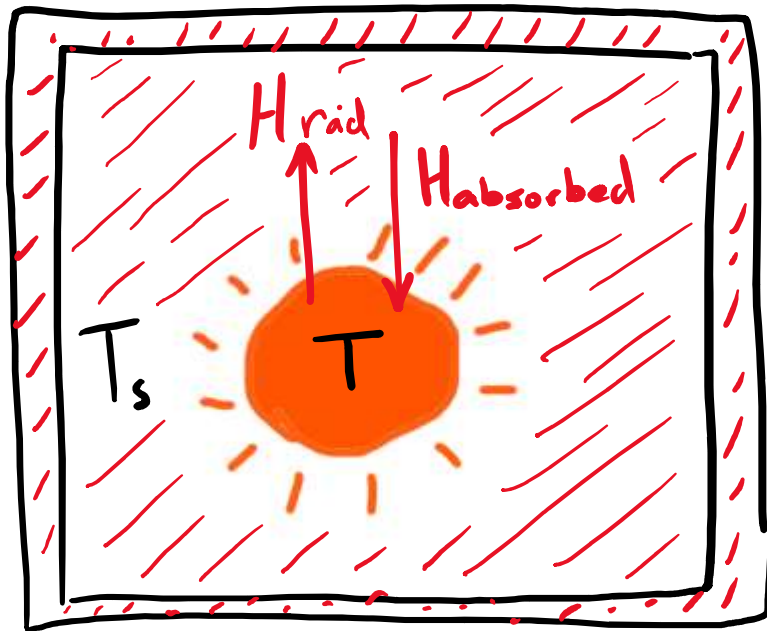
Stefan-Boltzmann constant

$$5.67 \times 10^{-8} \frac{\text{W}}{\text{m}^2 \cdot \text{K}^4}$$

$e = 1$  perfect absorber (black)

$e = 0$  perfect reflector (mirror)

# NET HEAT CURRENT FROM THERMAL RADIATION (in uniform temperature environment)



surface  
area

$$H_{rad} = A \cdot e \cdot \sigma \cdot T^4$$

$$H_{absorbed} = A e \sigma \cdot T_{surroundings}^4$$

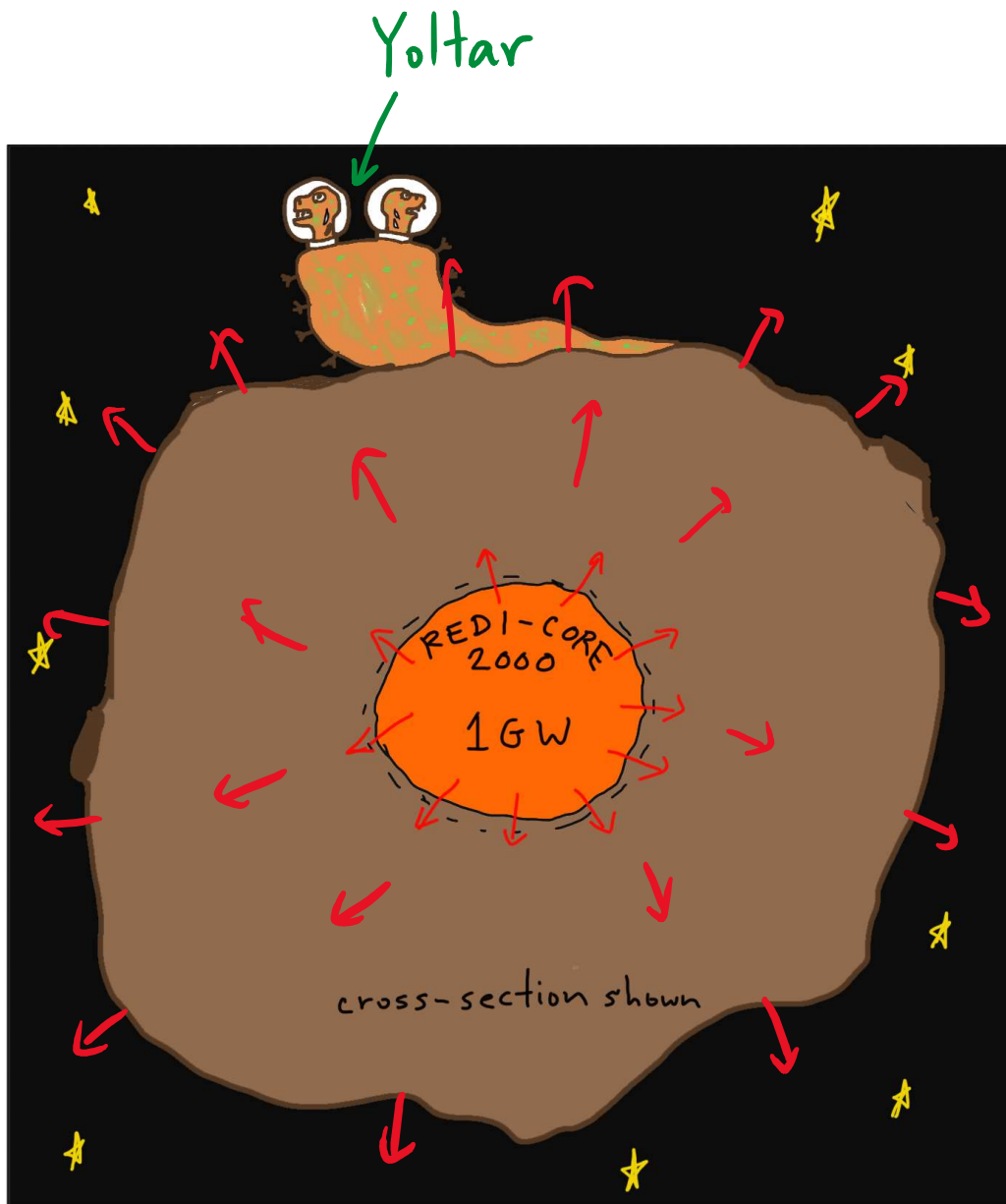
equilibrium:  $H_{absorbed} = H_{rad}$

Key relation for steady-state heat flow:

← temperatures not changing

$$H_{in} = H_{out}$$





Temperatures not  
changing



$$H_{in} = H_{out}$$

(for planet outside core)



$$P_{heater} = A \sigma e T^4$$



$$T_{surface} = \left( \frac{P_{heater}}{A \sigma e} \right)^{\frac{1}{4}}$$

A more interesting one...

A planet with radius  $r = 6400\text{km}$  lies at a distance  $R = 150,000,000\text{km}$  from a yellow star with temperature  $T = 5700\text{K}$  and radius  $R_s = 695,000\text{km}$ . **Estimate the surface temperature of the planet.**

The planet has **albedo** (fraction of incident light reflected)  $A = 0.37$  and emissivity  $e$  close to 1.

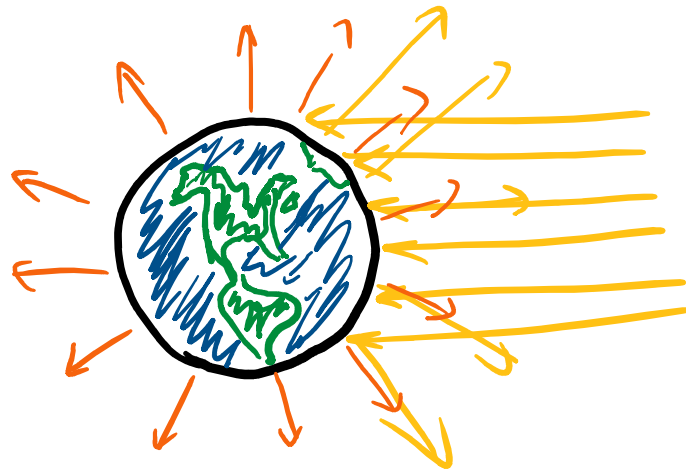


Key relation for steady-state heat flow:

$$H_{in} = H_{out}$$



Our problem:



$H_{in}$ : absorbed sunlight

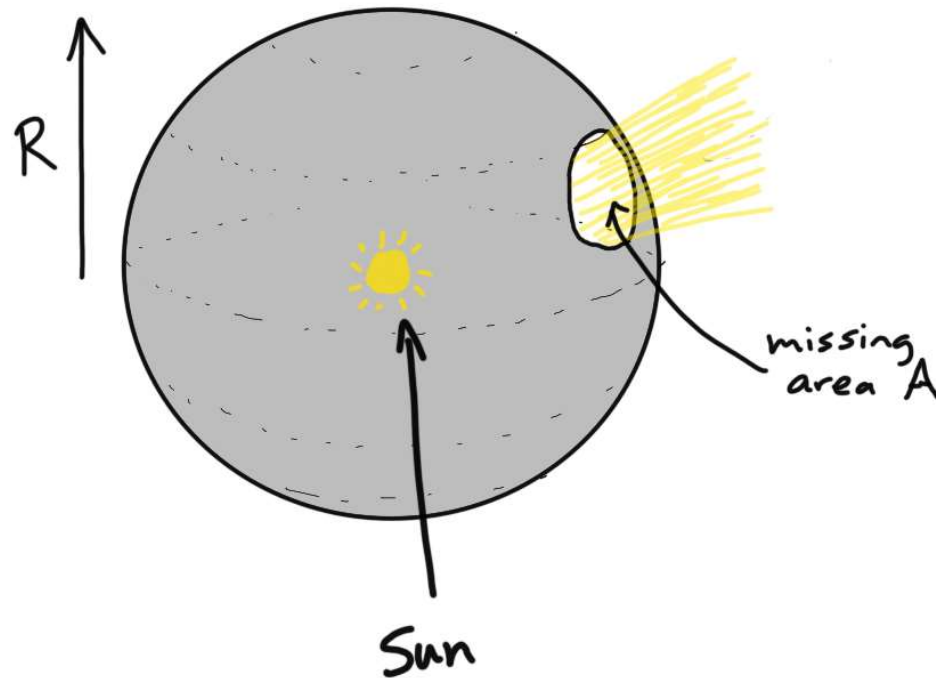
$H_{out}$ : IR radiation  
 $= A\epsilon\sigma T^4$

What is  $H_{in}$ ?



A gigantic sphere with radius  $R$  is built surrounding the sun. A hole is cut into the sphere, removing an area  $A$ . What is the rate of energy flow for light from the sun through the hole in terms of the Sun's total power  $H_{\text{sun}}$ ?

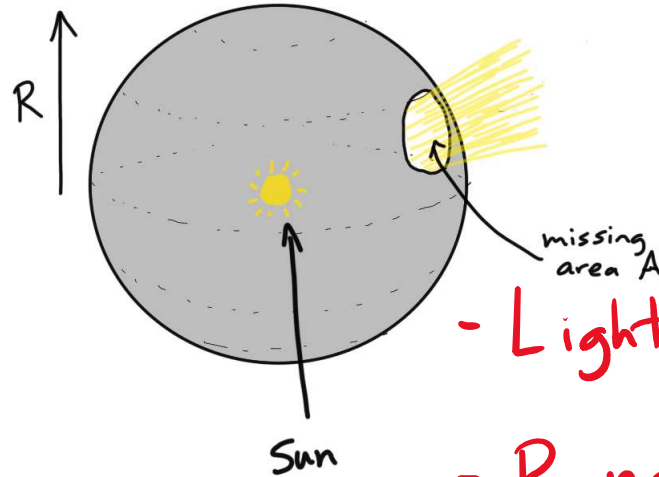
- A)  $H_{\text{Sun}} \times A$
- B)  $H_{\text{Sun}} \times \frac{A}{R^2}$
- C)  $H_{\text{Sun}} \times \frac{A}{\pi R^2}$
- D)  $H_{\text{Sun}} \times \frac{A}{4\pi R^2}$



**EXTRA:** If  $H_{\text{Sun}} = 3.86 \times 10^{26} \text{W}$  and  $R = 1.5 \times 10^{11} \text{m}$ , how much solar energy per second goes through an area of  $1 \text{m}^2$  at the distance  $R$ ?

A gigantic sphere with radius  $R$  is built surrounding the sun. A hole is cut into the sphere, removing an area  $A$ . What is the rate of energy flow for light from the sun through the hole in terms of the Sun's total power  $H_{\text{sun}}$ ?

- A)  $H_{\text{Sun}} \times A$
- B)  $H_{\text{Sun}} \times \frac{A}{R^2}$
- C)  $H_{\text{Sun}} \times \frac{A}{\pi R^2}$
- D)  $H_{\text{Sun}} \times \frac{A}{4\pi R^2}$



- Light spreads out uniformly
- Power leaving sun = power reaching sphere
- Hole covers fraction  $\frac{A}{4\pi R^2}$  of sphere

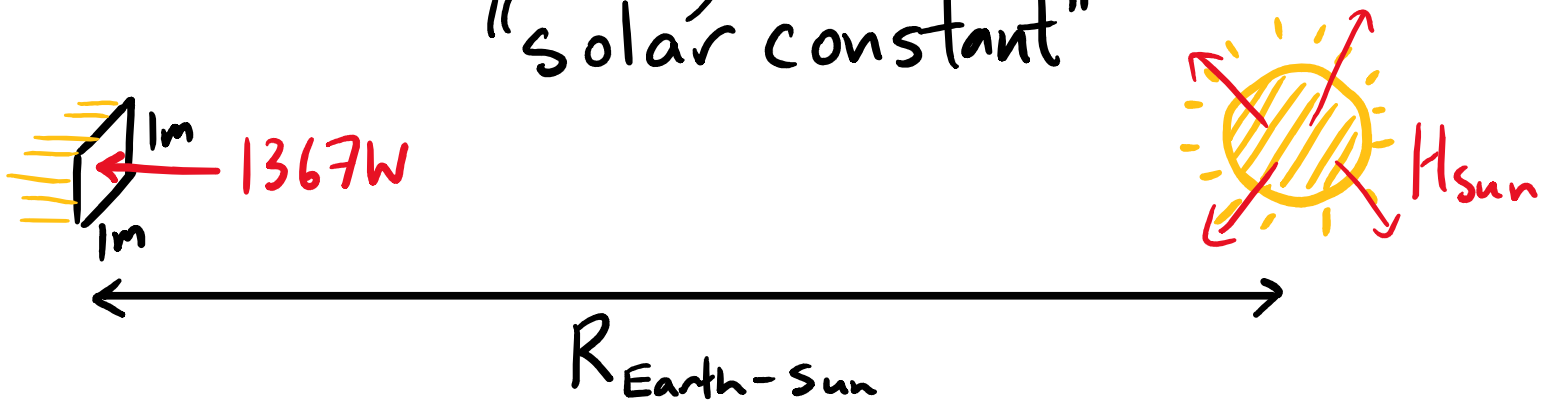
- So power of light coming out is  $\frac{A}{4\pi R^2} \times H_{\text{sun}}$

# The solar constant.

- The power from the Sun is  $H_{\text{Sun}} = A_{\text{Sun}} \cdot \sigma \cdot T_{\text{Sun}}^4$
- At Earth's orbit, the power per unit area (or INTENSITY) of sunlight is

$$I_{\text{sc}} = \frac{H_s}{4\pi R^2} = 1367 \text{ W/m}^2$$

"solar constant"



What is the power  $H_{in}$  of solar radiation absorbed by the Earth?  
Answer in terms of  $I_{sc}$ , the albedo  $a$  (fraction of sunlight reflected)  
and the Earth's radius  $r$ .



A)  $I_{sc} \cdot \pi r^2 \cdot a$

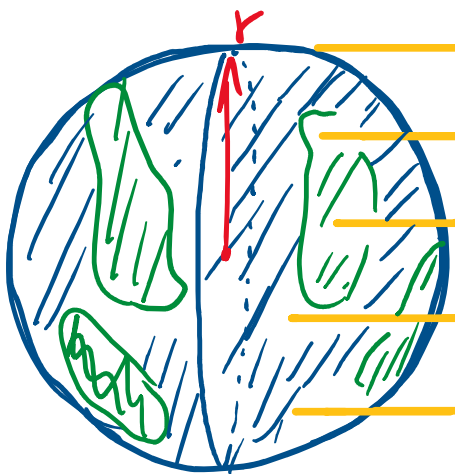
B)  $I_{sc} \cdot \pi r^2 \cdot (1-a)$

C)  $I_{sc} \cdot 2\pi r^2 \cdot a$

D)  $I_{sc} \cdot 2\pi r^2 \cdot (1-a)$

E)  $I_{sc} \cdot 4\pi r^2 \cdot (1-a)$

regular  
Earth



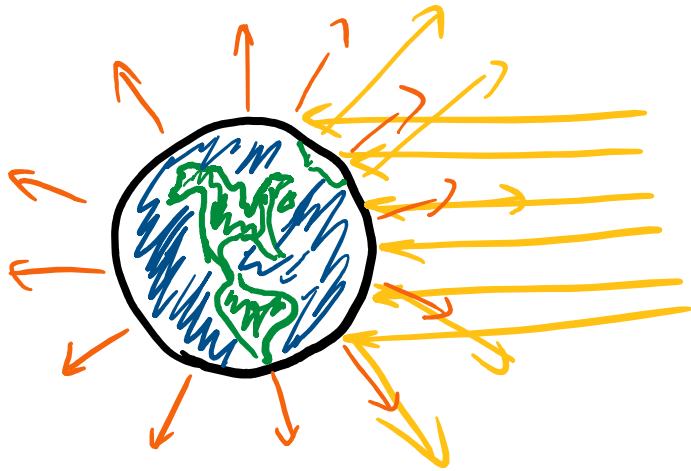
flat  
Earth



Each blocks same area of Sunlight:  $\pi r^2$

The heat current into the earth due to sunlight is  $H_{in} = \pi r^2 (1-a) I_{sc}$

Calculate the equilibrium surface temperature  $T$  in terms of  $a$ ,  $I_{sc}$ ,  $r$ ,  $\sigma$ , and the emissivity  $e$ .



$H_{in}$ : absorbed sunlight

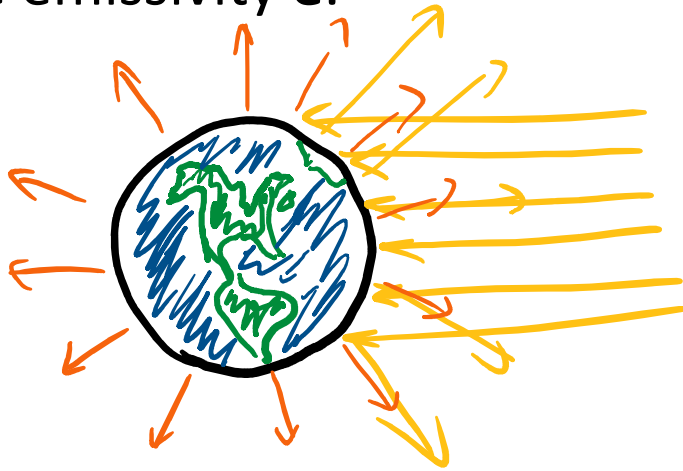
$H_{out}$ : IR radiation

recall:

$$H_{rad} = Ae\sigma T^4$$

The heat current into the earth due to sunlight is  $H_{in} = \pi r^2 (1-a) I_{sc}$

Calculate the equilibrium surface temperature  $T$  in terms of  $a$ ,  $I_{sc}$ ,  $r$ ,  $\sigma$ , and the emissivity  $e$ .



$H_{in}$ : absorbed sunlight

$H_{out}$ : IR radiation

The heat current into the earth due to sunlight is  $H_{in} = \pi r^2 (1-a) I_e$

Calculate the equilibrium surface temperature  $T$  in terms of  $a$ ,  $I_{sc}$ ,  $r$ ,  $\sigma$ , and the emissivity  $e$ .



We have  $H_{in} = H_{out}$  (steady state)

$$\pi r^2 (1-a) I_{sc} = 4\pi r^2 \cdot e \cdot \sigma \cdot T^4$$

$$\star T = \left[ \frac{(1-a) I_{sc}}{4e\sigma} \right]^{\frac{1}{4}} \star$$



$$\star T = \left[ \frac{(1-a)I_{sc}}{4e\sigma} \right]^{\frac{1}{4}} \star$$

The numbers: surface of the Earth has  $e \approx 1$  for IR radiation.

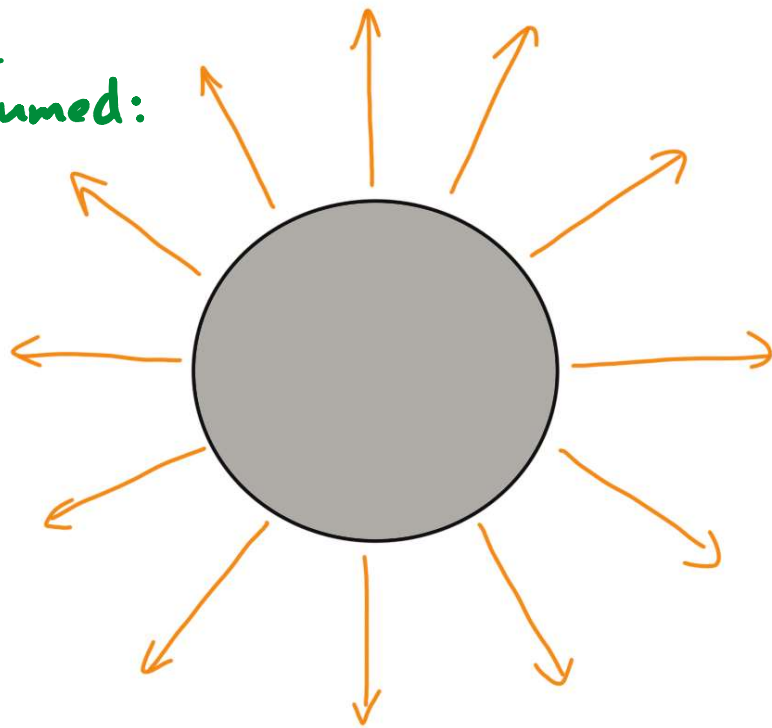
$$I_e = 1367 \text{ W/m}^2 \quad a \approx 0.3 \quad \sigma = 5.67 \times 10^{-8} \frac{\text{W}}{\text{m}^2 \text{K}^4}$$

These give  $T \approx -18^\circ\text{C}$

Something is off...

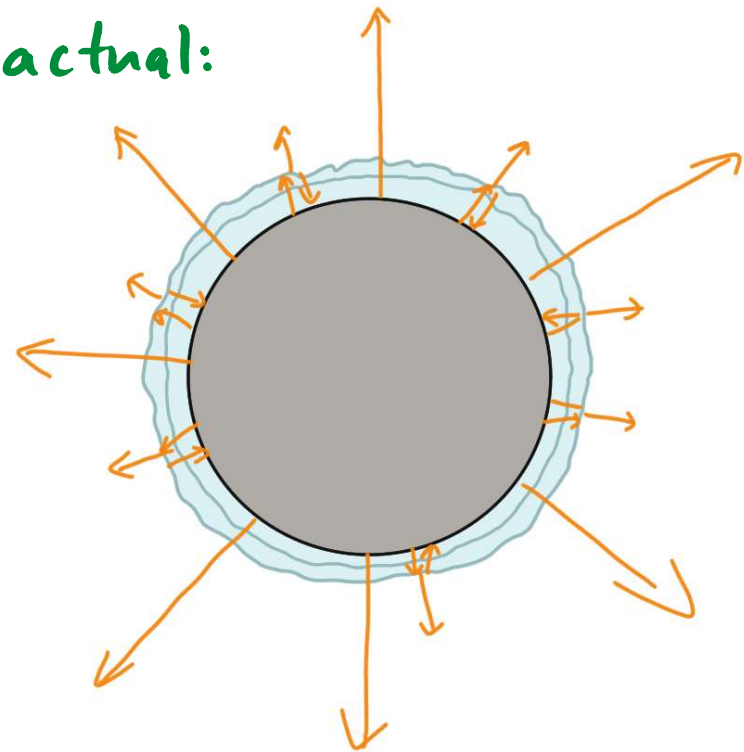
Actual surface temperature is larger due to the  
**GREENHOUSE EFFECT**: some IR radiation is  
absorbed by "greenhouse gases" + re-emitted back to  
Earth.

we  
assumed:



$e = 1$

actual:



$e \approx 0.6$

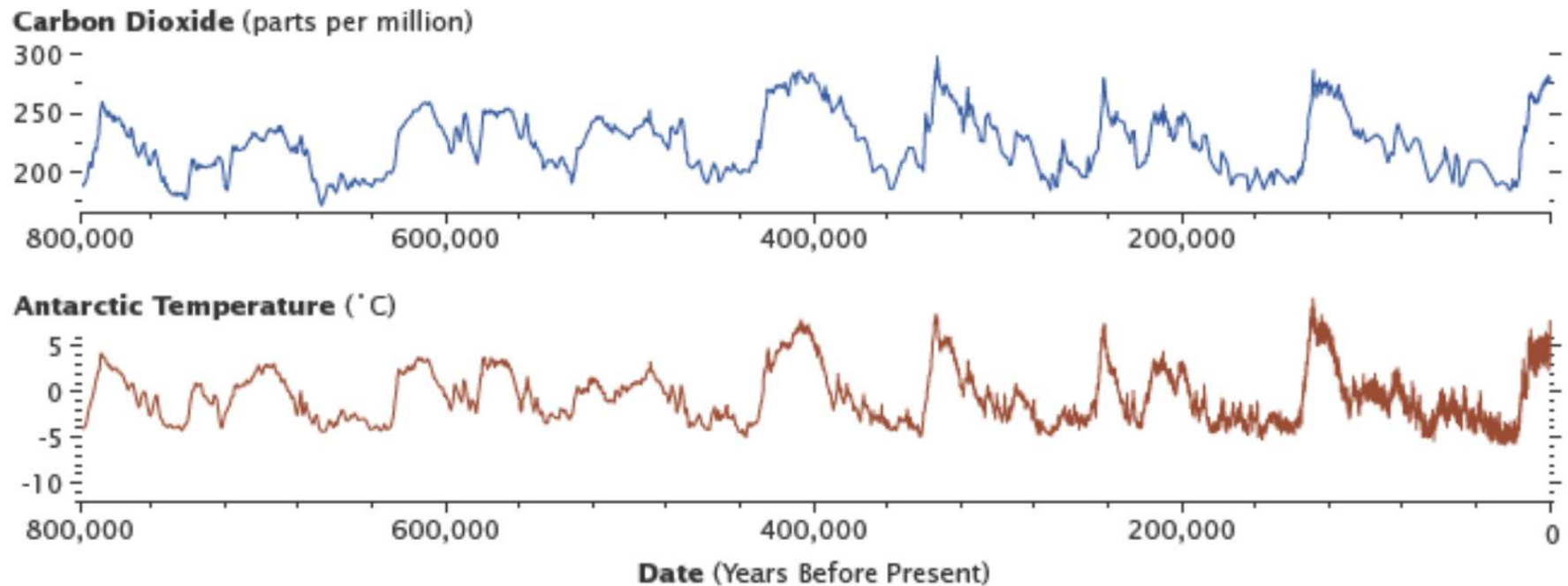
$$\star T = \left[ \frac{(1-a)I_{sc}}{4e\sigma} \right]^{\frac{1}{4}} \star$$

Lower  $e \Rightarrow$  higher  $T$

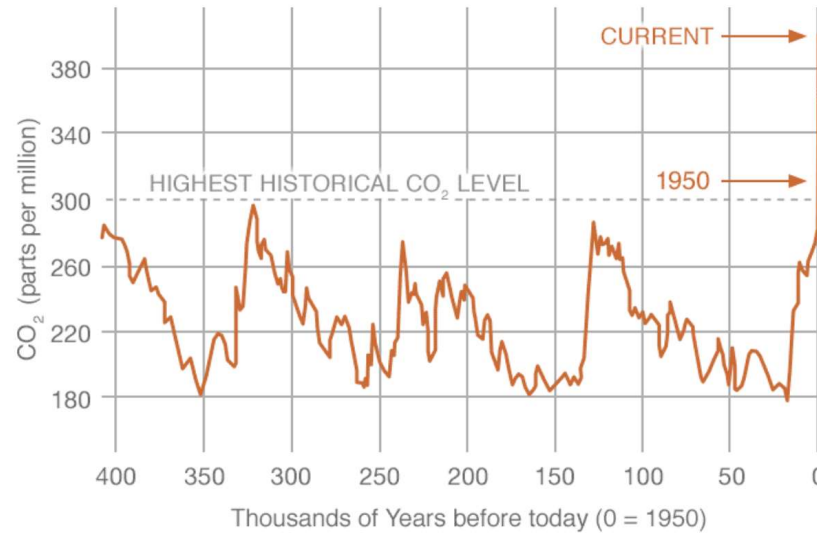
Real  $e \approx 0.6$  gives  $T = 14.5^\circ\text{C}$

But  $e$  can decrease e.g. due to increasing  $\text{CO}_2$  concentration in atmosphere.  $\longrightarrow$  Global warming

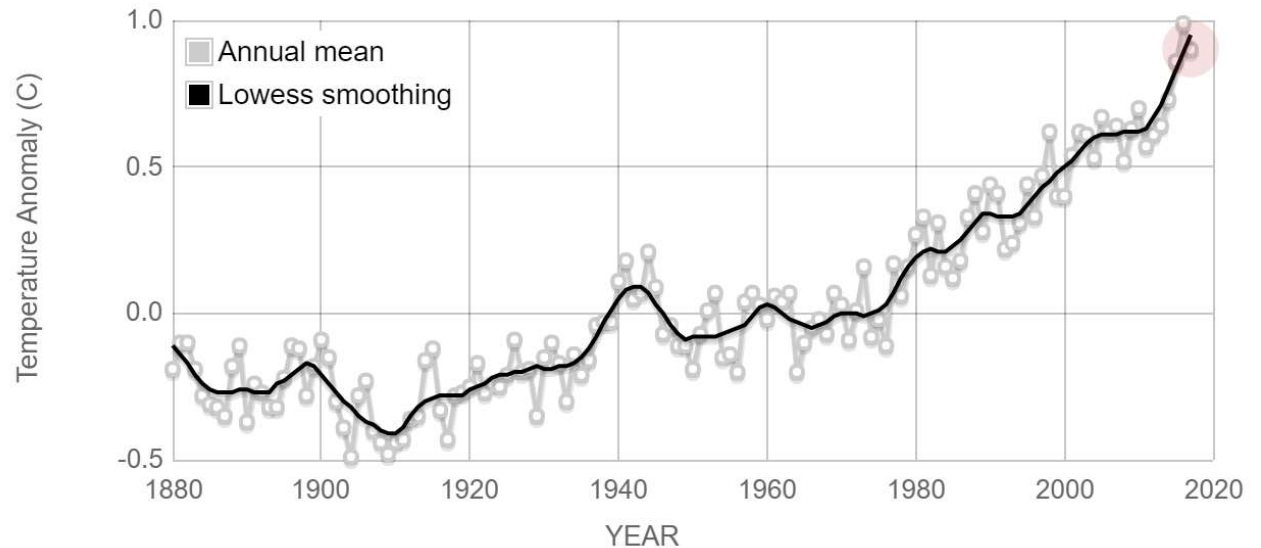
CO<sub>2</sub> correlates closely with temperature



CO<sub>2</sub> levels:



Temperature:



Almost all climate scientists believe this rise due to human activity